VI. Further Experiments upon the Blood Volume of Mammals and its Relation to the Surface Area of the Body.

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In previous papers* we have shown that the blood volume of normal and healthy mammals, such as rabbits, guinea-pigs, and mice, is satisfactorily expressed by the formula $B = W^n/k$, where B is the blood volume in cubic centimetres, W the weight of the individual in grammes, n approximately $\frac{2}{3}$, and k a constant (calculated from the experiments), which varies with the particular species of animal. This formula indicates that the smaller and lighter animals of any given species, which have a relatively greater body surface than the heavier ones, have also a relatively greater blood volume—in other words, the blood volume can be expressed as a function of the body surface, and it must therefore be misleading to express it in per cent. of the body weight, since when so expressed it is not a constant for any given species of mammal.

As it was of interest to ascertain whether wild animals of closely allied species would differ greatly as regards their blood volume from the above-mentioned tame animals, we have determined the blood volume of hares, wild rabbits, and wild rats.

Technique.—The animals were used for the experiments immediately, or within a few days of capture. In the case of the hare and wild rabbit, the blood volume was determined by washing out the circulatory system with oxygenated Locke's fluid according to the method given in our last paper, and in the wild rat, by Welcker's method, modified as described in the same paper.

In all the tables, as in our previous paper, the weight of the animals is "Rohgewicht" in grammes, *i.e.*, the weight of the contents of the alimentary canal is not deducted: the blood volume is given in cubic centimetres, and the hæmoglobin is expressed as a percentage of the amount normal in man (man=100 per cent.).

In Table I are given the experimental results of the determination of the blood volume of five hares of weights varying from 2550 to 3780 grms., as well as * Vide references at end.

the values for the blood constant $k = W^{\sharp}/B$, and the ratio of the blood volume to body weight expressed as a percentage of the latter.

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TABL	Tr I
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No.	Sex	Body weight. ("Rohgewicht.")	Hæmoglobin per cent. (Man = 100.)	Blood volume observed.	Blood constant, $k \ (= W^{\frac{2}{3}}/B).$	Blood volume as percentage of body weight.
1 2 3 4 5	50505050	grammes. 2550 2670 2680 2960 3780	$115 \cdot 2$ $98 \cdot 8$ $115 \cdot 9$ $116 \cdot 2$ $114 \cdot 6$	$\begin{array}{c} \text{c.e.} \\ 192 \cdot 0 \\ 216 \cdot 2 \\ 215 \cdot 0 \\ 220 \cdot 0 \\ 242 \cdot 0 \end{array}$	$ \begin{array}{c} 0 \cdot 97 \\ 0 \cdot 89 \\ 0 \cdot 90 \\ 0 \cdot 94 \\ 1 \cdot 00 \end{array} $	$7 \cdot 53$ $8 \cdot 10$ $8 \cdot 02$ $7 \cdot 43$ $6 \cdot 40$
		Average	112·1		0.94	7.50

It is seen that the blood constant exhibits relatively small non-periodic deviations, and hence that, as shown in our previous communications, the lighter animals have a greater percentage of blood than the heavier ones. The average value of k is 0.94, and the average percentage 7.50.

TABLE II.

No.	Body weight. ("Rohgewicht.")	Blood volume observed.	Blood volume calculated. $B = W^{\frac{3}{4}}/k$. $(k = 0.94.)$	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (7·50) of body weight.	Difference between blood volume calculated and observed.
1 2 3 4 5	grammes. 2550 2670 2680 2960 3780	$\begin{array}{c} \text{c.c.} \\ 192 \cdot 0 \\ 216 \cdot 2 \\ 215 \cdot 0 \\ 220 \cdot 0 \\ 242 \cdot 0 \end{array}$	$\begin{array}{c} \text{c.c.} \\ 198 \cdot 6 \\ 204 \cdot 7 \\ 205 \cdot 2 \\ 219 \cdot 4 \\ 258 \cdot 1 \end{array}$	$\begin{array}{c} \text{per cent.} \\ 3 \cdot 32 \\ 5 \cdot 62 \\ 4 \cdot 78 \\ 0 \cdot 27 \\ 6 \cdot 24 \end{array}$	$\begin{array}{c} \text{c.c.} \\ 191 \cdot 2 \\ 200 \cdot 2 \\ 201 \cdot 0 \\ 222 \cdot 0 \\ 283 \cdot 0 \end{array}$	$\begin{array}{c} \text{per cent.} \\ 0 \cdot 42 \\ 7 \cdot 99 \\ 6 \cdot 97 \\ 0 \cdot 90 \\ 14 \cdot 49 \end{array}$
		A	verage	4.05		6 · 15

In Table II it will be seen that the average deviation between the calculated and observed figures is only 4.05 per cent. if the blood volume is calculated as a function of the surface, while it is 6.15 per cent. when calculated as a percentage of the body weight.

In Tables III, IV, V, and VI are given the results of our experiments upon the blood volume of 11 wild rabbits, ranging in weight from 1195 to 1570 grms. In

Table III are given the blood volumes and the hæmoglobin percentages, as well as the blood constant $k = W^3/B$ and the blood volume expressed as percentage of body weight.

TABLE III.

No.	Sex.	Body weight. ("Rohgewicht.")	Hæmoglobin per cent. (Man = 100.)	Blood volume observed.	Blood constant, $k = W^{\frac{2}{3}}/B$).	Blood volume as percentage of body weight.
1 2 3 4 5 6 7 8 9 10	\$ 40 to \$ 40 to 40 to 40 to	grammes. 1195 1350 1350 1390 1440 1450 1480 1500 1520 1550 1570	$93 \cdot 0$ $89 \cdot 6$ $81 \cdot 2$ $75 \cdot 3$ $83 \cdot 0$ $80 \cdot 6$ $94 \cdot 7$ $82 \cdot 9$ $97 \cdot 3$ $88 \cdot 1$ $82 \cdot 2$	$\begin{array}{c} \textbf{c.c.} \\ \textbf{54} \cdot 8 \\ \textbf{56} \cdot 0 \\ \textbf{61} \cdot 0 \\ \textbf{64} \cdot 0 \\ \textbf{64} \cdot 5 \\ \textbf{61} \cdot 9 \\ \textbf{67} \cdot 0 \\ \textbf{61} \cdot 3 \\ \textbf{62} \cdot 8 \\ \textbf{71} \cdot 0 \\ \textbf{64} \cdot 5 \\ \end{array}$	$2 \cdot 05$ $2 \cdot 18$ $2 \cdot 00$ $1 \cdot 95$ $1 \cdot 98$ $2 \cdot 07$ $1 \cdot 94$ $2 \cdot 14$ $2 \cdot 10$ $1 \cdot 89$ $2 \cdot 10$	$4 \cdot 59$ $4 \cdot 15$ $4 \cdot 52$ $4 \cdot 60$ $4 \cdot 48$ $4 \cdot 27$ $4 \cdot 53$ $4 \cdot 09$ $4 \cdot 13$ $4 \cdot 58$ $4 \cdot 11$
	, and a second of the second	Average	86 · 2		2.04	4 · 37

The average blood constant is 2.04, and the average percentage of blood to body weight is 4.37.

Table IV.

No.	Body weight. ("Rohgewicht.")	Blood volume observed.	Blood volume calculated. B = $W^{\frac{3}{6}}/k$. ($k = 2.04$).	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (4·37) of body weight.	Difference between blood volume calculated and observed.
			-			
1	grammes. 1195	6.c. 54·8	c.c. 55 · 2	$\begin{array}{c} \text{per cent.} \\ 0.72 \end{array}$	$\begin{array}{c} \text{c.c.} \\ 52 \cdot 2 \end{array}$	per cent. 4 · 98
1 -	1350	56.0	59.9	$\frac{0.72}{6.51}$	$59 \cdot 0$	5.08
$\frac{2}{3}$				$\frac{6.91}{1.84}$	59.0	3.39
	1350	61.0	59.9		$\frac{59}{60.7}$	5 · 44
4	1390	64.0	61 · 1	4.75		$\frac{5.44}{2.54}$
5	1440	64.5	62.5	$\frac{3\cdot 20}{1\cdot 42}$	$62 \cdot 9$	
6	1450	61.9	62.8	1.43	63.4	2:37
7	1480	67.0	63.7	5.18	$64 \cdot 7$	3.55
8	1500	61.3	64.2	4.52	65.5	6:41
	1520	62.8	64.8	3.09	66 · 4	5 · 42
10	1550	71.0	65 · 7	8.07	$67 \cdot 7$	4.87
11	1570	64.5	66 · 2	$2\cdot 57$	68.6	5:98
Auto a Character of the Control of t	-	A	verage	3.81		4.55

In Table IV the blood volume, as calculated from the average blood constant k (2.04), and from the average percentage (4.37), is given. It will be seen that the VOL. CCII.—B. 2 B

average deviation between the calculated and observed figures in the former case is 3.81 per cent., while in the latter it is 4.55 per cent.

Group.	Rabbits from Table III included in group.	Average body weight. (" Rohgewicht.")	Average blood volume observed.	Blood constant,* $k \ (= W^{3}/B).$	Blood volume* expressed as percentage of body weight.
A B C D	1 24 58 911	grammes. 1195 1363 1468 1547	$\begin{array}{c} \text{c.c.} \\ 54 \cdot 8 \\ 60 \cdot 3 \\ 63 \cdot 7 \\ 66 \cdot 1 \end{array}$	$2 \cdot 05$ $2 \cdot 04$ $2 \cdot 03$ $2 \cdot 02$	$\begin{array}{c} \text{c.c.} \\ 4 \cdot 59 \\ 4 \cdot 42 \\ 4 \cdot 34 \\ 4 \cdot 27 \end{array}$
and have the first of the foreign days are necessarians.			Average	2.04	4.41

TABLE V.

^{*} The figures in these columns are calculated from the average body weight and the average blood volume of the group.

Group.	Rabbits from Table III included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood volume calculated. $B = W^{8}/k$. (Average k for the groups, 2.04.)	Difference between blood volume calculated and observed.	Blood volume calculated as percentage of body weight. (Average for the groups, 4.41.)	Difference between blood volume calculated and observed.
A B C D	1 2—4 5—8 9—11	grammes. 1195 1363 1468 1547	c.c. 54·8 60·3 63·7 66·1	c.c. 55·2 60·3 63·3 65·6	per cent. 0·72 0·00 0·63 0·76	c.c. 52·7 60·1 64·7 68·2	per cent. 4 · 74 0 · 33 1 · 55 3 · 08

Table VI.

In Table V the experiments upon wild rabbits are arranged in four groups by averaging the weights and blood volumes of the animals in each group. The average blood constant is 2.04, while the average blood as percentage of body weight is 4.41. In Table VI is calculated the blood volume from the average blood constants of the groups (2.04), and from the average percentage (4.41) of the groups, and the percentage deviation between the calculated and observed values in each case is also given.

In the first case the deviation is only 0.53 per cent., whilst in the second it is 2.43 per cent. Here, as before, it is obvious that our formula represents the

experimental facts in a more satisfactory way than if the blood volume be calculated as percentage of the body weight, as has hitherto been usual.

In Tables VII, VIII, IX, and X are detailed the results of our experiments upon the blood volume of six wild rats, ranging in weight from 228 to 436 grms.

TABLE VII.

No.	Body weight. ("Rohgewicht.")	Hæmoglobin per cent. (Man = 100.)	Blood volume observed.	Blood constant, $k = W^{\frac{3}{2}}/B$).	Blood volume as percentage of body weight.
	grammes.		C.C.		
1	228	$85 \cdot 3$	$12\cdot 02$	3.10	$5\cdot 27$
2	256	$85 \cdot 7$	$12 \cdot 43$	$3\cdot 24$	$4 \cdot 86$
3	277	$67 \cdot 3$	$14 \cdot 99$	$2 \cdot 83$	5.41
4	292	$70 \cdot 6$	$14 \cdot 92$	$2 \cdot 95$	5.11
5	326	$75 \cdot 8$	$14 \cdot 85$	$3 \cdot 19$	$4\cdot 56$
6	436	$78 \cdot 5$	$19\cdot 45$	2 · 96	4 · 46
·	Average	$77 \cdot 2$		3.05	4.81

In Table VII are given the blood volumes and hæmoglobin percentages, as well as the values of the blood constant $k = W^{\sharp}/B$, and the blood volumes expressed as percentage of the body weight. The average blood constant is 3.05, and the average percentage 4.81. It is seen, as usual, that although the blood constant varies only slightly and without periodicity, the ratio of blood volume to body weight decreases markedly, and more or less regularly, as the animals increase in weight.

TABLE VIII.

No.	Body weight. ("Rohgewicht.")	Blood volume observed.	Blood volume calculated. $B = W^{\frac{3}{2}}/k.$ $(k = 3.05.)$	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (4·81) of body weight.	Difference between blood volume calculated and observed.
	grammes.	c.c.	c.c.	per cent.	c.c.	per cent.
1	228	12:02	12.24	1.80	10.97	9.57
$\overline{2}$	256	12.43	$13 \cdot 22$	5.98	$12 \cdot 31$	0.97
3	$\frac{1}{277}$	14.99	$13 \cdot 93$	$7 \cdot 61$	$13 \cdot 32$	12.54
4	292	14.92	14.43	3 · 40	$14 \cdot 04$	$6 \cdot 27$
5	326	14.85	15.53	$4 \cdot 38$	15.68	$5\cdot 29$
6	436	19.45	18.86	$3 \cdot 13$	$20 \cdot 97$	$7\cdot 25$
American management		A	verage	4.38		6.98

Table VIII represents the blood volume calculated from the average blood constant (3.05), and from the average percentage (4.81). The average deviation between the

calculated and observed figures is, when calculated according to our formula, 4.38 per cent., whilst if calculated as percentage of body weight it is 6.98 per cent.

Group.	Rats from Table VII included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood constant,* $k \ (= W^{3}/B).$	Blood volume* expressed as percentage of body weight.
A B C D	1 2 and 3 4 and 5 6	grammes, 228 267 309 436	$\begin{array}{c} \text{c.c.} \\ 12 \cdot 02 \\ 13 \cdot 71 \\ 14 \cdot 89 \\ 19 \cdot 45 \end{array}$	$3 \cdot 10$ $3 \cdot 02$ $3 \cdot 07$ $2 \cdot 96$	$5 \cdot 27$ $5 \cdot 13$ $4 \cdot 82$ $4 \cdot 46$
Particular Publisher Particular P	T .		Average	3.04	4.92

TABLE IX.

In Table IX the rats are arranged in four groups according to weight, and the blood constant and blood percentage calculated from the average figures of these groups. Again it will be seen that while the constant varies slightly and without marked periodicity, the blood percentage falls regularly from 5.27 per cent. in the lightest group to 4.46 per cent. in the heaviest.

TABLE X.

Group.	Rats from Table VII included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood volume calculated. B = $W^{\frac{3}{2}}/k$. (Average k for the groups, 3.04.)	Difference between blood volume calculated and observed.	Blood volume calculated as percentage of body weight. (Average for the groups, 4.92.)	Difference
	the contract of the contract o	grammes.	c.c.	c.c.	per cent.	c.c.	per cent.
\mathbf{A}	1	228	12.02	$12 \cdot 28$	$2 \cdot 12$	$11 \cdot 22$	$7 \cdot 13$
В	2 and 3	267	13.71	13.64	0.51	13.14	4 · 34
C	4 and 5	309	14.89	15.03	0.93	$15 \cdot 20$	2:04
D	6	436	19.45	18.92	$2 \cdot 80$	$21 \cdot 45$	$9 \cdot 32$
			Av	erage	1.59		5.71

In Table X the blood volume is calculated from the average constant k of the groups (3.04), and from the average percentage of the groups (4.92 per cent.). At the same time is given the percentage deviation between the calculated and

^{*} The figures in these columns are calculated from the average body weight and average blood volume of the group.

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observed figures in each case. The average percentage deviation between the calculated and observed figures is 1.59 per cent. if the blood volume be calculated according to our view, while it is 5.71 per cent. if expressed as percentage of the body weight.

Our experiments upon freshly-caught normal and healthy mammals which have lived in a natural state, such as hares, wild rabbits, and wild rats, therefore prove as clearly as did our experiments upon the tame rabbit, guinea-pig, and mouse, that our formula $B = W^{3}/k$ (indicating that the blood volume is a function of the surface) holds good, and represents the experimental facts in an extremely satisfactory manner. At the same time it is obvious from these experiments that the blood volume as percentage of body weight is, in any given species of the animals investigated, anything but a constant, and that any attempt to express it as such must be misleading and tend to obscure an important truth.

TABLE XI.

Species.	Range of weight. (" Rohgewicht.")	Average difference between blood volume calculated and observed. $B = W^{\frac{1}{8}}/k$.	Average difference between blood volume calculated and observed. B = per cent. body weight.	Heaviest animal in terms of the lightest.	Difference according to weight in terms of difference according to surface.
Tame rabbit Guinea-pig . Mouse Hare Wild rabbit. Wild rat	$ \begin{array}{r} 215 - 825 \\ 11 \cdot 90 - 29 \cdot 35 \\ 2550 - 3780 \end{array} $	per cent. $4 \cdot 61$ $4 \cdot 57$ $6 \cdot 65$ $4 \cdot 05$ $3 \cdot 81$ $4 \cdot 38$	per cent. $9 \cdot 11$ $9 \cdot 27$ $8 \cdot 61$ $6 \cdot 15$ $4 \cdot 55$ $6 \cdot 98$	$4 \cdot 85$ $3 \cdot 84$ $2 \cdot 47$ $1 \cdot 48$ $1 \cdot 31$ $1 \cdot 91$	$1 \cdot 90$ $2 \cdot 03$ $1 \cdot 29$ $1 \cdot 52$ $1 \cdot 19$ $1 \cdot 59$
	Average	4.68	7:45		1.60

In Table XI are given the different species of animals upon which we have determined the blood volume, the range of their weights, and the average differences between the blood volume calculated, (a) as a function of the surface, and (b) as percentage of the body weight, and the observed figures. This table refers to the individual experiments, and the figures given have been calculated from the average k and from the average percentages of the individuals of each species. From this table it is clearly seen that in every case the average percentage difference between calculated and observed figures is much greater when the blood volume is calculated as percentage of the body weight than when calculated as a function of the surface. In the former case the average percentage difference between the calculated and the observed figures of the six species is 7.45 per cent., whilst in the latter it is only 4.68 per cent. At the same time it is seen that when the blood volume is calculated as percentage of body weight, the greater the range of weight of the animals

experimented upon the greater is the average difference between the calculated and observed values. This is not the case if the blood volume be calculated as a function of the surface.

As it is obvious that the percentage difference between the values calculated by the two methods and the values observed depends largely not only upon the actual range of weight of the animals, but also on the relative number of large and small animals, the actual difference between the two methods of calculation is brought out much more definitely by grouping together the animals of approximately the same weight within the same species.

TABLE XII.

Species.	Range of average weight of groups.	Average difference between blood volume calculated and observed. $B = W^{\frac{3}{8}/k}.$	Average difference between blood volume calculated and observed. B = per cent. body weight.	Heaviest group in terms of the lightest.	Difference in blood volume according to weight in terms of difference according to surface.
Tame rabbit Guinea-pig . Mouse Wild rabbit. Wild rat	$\begin{array}{c} \text{grammes.} \\ 670-3039 \\ 245-825 \\ 12\cdot 94-25\cdot 84 \\ 1195-1547 \\ 228-436 \end{array}$	$\begin{array}{c} \text{per cent.} \\ 2 \cdot 77 \\ 1 \cdot 92 \\ 1 \cdot 35 \\ 0 \cdot 53 \\ 1 \cdot 59 \end{array}$	$\begin{array}{c} \text{per cent.} \\ 11 \cdot 91 \\ 10 \cdot 87 \\ 6 \cdot 38 \\ 2 \cdot 43 \\ 5 \cdot 71 \end{array}$	$egin{array}{c} 4 \cdot 54 \\ 3 \cdot 37 \\ 2 \cdot 00 \\ 1 \cdot 29 \\ 1 \cdot 91 \end{array}$	$4 \cdot 30$ $5 \cdot 66$ $4 \cdot 73$ $4 \cdot 58$ $3 \cdot 59$
	Average	2 · 16	8 · 43		4.57

Accordingly in Table XII are given, for the different species, the average percentage deviations between the blood volumes calculated from the average blood constant for the groups and the average blood percentage of the groups for each species, and the observed values.

It is at once seen that if the blood volume be calculated as a function of the surface, the average percentage deviation is 2·16, whilst if it be calculated as percentage of body weight it is 8·43 per cent., or practically *four* times as great. At the same time it is seen that the greater the range of weight of the animals experimented upon the more misleading and erroneous it is to express the blood volume as a given percentage of the body weight.

The blood constants from which the blood volume of the normal healthy mammal can be calculated if the "Rohgewicht" of the animal is known, according to our formula $B = W^{\frac{3}{2}}/k$, are for the

Tame rabbit			1.58	Hare			0.94
Guinea-pig			3.30	Wild rabbit			2.04
Mouse			6.70	Wild rat .			3.05

From these figures it is clear that a wild rabbit contains about 25 per cent. less blood in its circulatory system than a tame rabbit of exactly the same weight, while at the same time the percentage of hæmoglobin in its blood is nearly 25 per cent. more than in the tame variety. It is also interesting to note that if we compare a wild rabbit with a hare of the same weight, we find that the hare contains about 125 per cent. more blood, and that the percentage of hæmoglobin is about 30 per cent. greater.

As our experiments have shown that it is not only in animals constantly living in captivity, but also in animals of the same or closely allied species enjoying their natural life, that the blood volume is a function of the surface, it is interesting to ascertain if the blood volume continues to be a function of the surface under other conditions not interfering with the general health, but attended by a marked change in the blood volume, as, for example, in animals which have been transferred from a low to a high altitude.

Numerous and careful experiments upon the blood volume of rabbits at low and high altitudes have been carried out by E. ABDERHALDEN in his excellent work concerning the effects of high altitudes upon the number of red blood corpuscles, the percentage of hæmoglobin in the blood, and the blood volume, in tame rabbits.

We give below a brief account of Abderhalden's results when dealt with according to our view.

Tables XIII—XX give ABDERHALDEN'S results as to the blood volume of tame rabbits. The animals were derived from various stocks at Basle (266 metres above sea level) and transferred to St. Moritz (1856 metres above sea level), where, after four to eight and a half weeks, they were killed and their hæmoglobin percentage and blood volume determined.

Members of the same stock of animals remained in Basle to serve as controls, and a third group of members of the same stock were taken to St. Moritz, and after being kept there from four to eight weeks were brought back to Basle. Here their hæmoglobin percentage and blood volume were estimated after they had been back from 2 to 15 days.

Table XIII gives details of the weight, hamoglobin percentage, and blood volume observed by ABDERHALDEN. From these data we have calculated the blood constant from the formula $k = W^{\ddagger}/B$, and the blood volume as percentage of the body weight in the animals killed at St. Moritz. The average blood constant is found to be 1.78, while the average figure representing the blood as percentage of body weight is 4.34. Here, again, it is seen that while the blood constant does not vary markedly according to the weight of the animal, the blood volume expressed as a percentage of body weight varies in the usual way, in that the smaller and lighter rabbits contain relatively more blood per unit of body weight than do the heavier ones.

No.	Reference in ABDER- HALDEN'S paper.	Sex.	Body weight. ("Rohgewicht.")	Blood volume observed.	Hæmoglobin (as given by ABDER- HALDEN).	Blood constant, $k (=\mathrm{W}^{\frac{3}{3}}/\mathrm{B}).$	Blood volume as percentage of body weight.
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19	X 2 IX 6 XI 1 XI 2 III 4 VII 7 VII 3 VI 4 VI 2 IX 5 VIII 1 IV 6 VIII 7 III 1 IV 4 VII 2 III 1 IV 6 VIII 7	04,000,000,000,000,000,000,000,000,000	grammes. 1200 1620 1649 1710 1928 2120 2120 2176 2175 2215 2457 2609 2615 2641 2715 2840 2875 2900 3112	$\begin{array}{c} \text{c.c.} \\ 60 \cdot 3 \\ 81 \cdot 0 \\ 76 \cdot 3 \\ 76 \cdot 2 \\ 88 \cdot 8 \\ 88 \cdot 8 \\ 98 \cdot 1 \\ 87 \cdot 8 \\ 113 \cdot 9 \\ 97 \cdot 6 \\ 89 \cdot 8 \\ 113 \cdot 8 \\ 87 \cdot 1 \\ 121 \cdot 6 \\ 103 \cdot 2 \\ 124 \cdot 2 \\ 112 \cdot 2 \\ 116 \cdot 8 \\ 124 \cdot 5 \\ \end{array}$	$\begin{array}{c} 13 \cdot 41 \\ 13 \cdot 81 \\ 14 \cdot 22 \\ 14 \cdot 77 \\ 14 \cdot 05 \\ 14 \cdot 87 \\ 12 \cdot 96 \\ 15 \cdot 32 \\ 15 \cdot 77 \\ 14 \cdot 71 \\ 15 \cdot 41 \\ 16 \cdot 12 \\ 16 \cdot 22 \\ 14 \cdot 56 \\ 15 \cdot 22 \\ 14 \cdot 29 \\ 14 \cdot 45 \\ 14 \cdot 09 \\ 14 \cdot 92 \\ \end{array}$	1·87 1·70 1·83 1·87 1·74 1·86 1·68 1·91 1·47 1·74 2·03 1·66 2·18 1·57 1·88 1·62 1·80 1·74 1·71	5·03 5·00 4·63 4·46 4·61 4·19 4·63 4·05 5·24 4·54 3·65 4·36 3·33 4·60 3·80 4·37 3·90 4·03 4·00
			Avera	ge	14:69	1 · 78	4.34

TABLE XIII*.

In Table XIV we have calculated the blood volume from the average blood constant (1.78), and from the average percentage (4.34). At the same time, the difference between the calculated and observed figures is given in per cent. according to the two methods. The average percentage deviation is seen to be 7.01 per cent., if the blood volume be calculated as a function of the surface, while it is 8.21 per cent. if it be calculated as percentage of body weight.

In Table XV we have arranged the animals in four groups according to their weights, giving a range in weight from 1545 to 2888 grms., and the average blood volumes of the groups. There is also given the blood constant $k = W^3/B$, and the blood volume as percentage of body weight. Here, again, it is seen that the blood constant does not vary greatly as the groups increase in weight, although the percentage of blood to body weight decreases regularly from 4.92 to 4.02 per cent.

In Table XVI is calculated the blood volume, from the average blood constant of the groups (1.76), and also from the blood as percentage of body weight (percentage = 4.39). There are also shown the percentage differences between the

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

TABLE XIV*.

No.	Reference in ABDER- HALDEN'S paper.	Sex.	Body weight. ("Rohgewicht.")	Blood volume observed.	Blood volume calculated. $B = W^{\frac{1}{6}}/k.$ $(k = 1.78.)$	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (4·34) of body weight.	Difference between blood volume calculated and observed.
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 19	X 2 IX 6 XI 1 XI 2 III 4 VII 7 VII 3 VI 4 VI 2 IX 5 VIII 1 IV 6 VIII 7 III 1 IV 4 II 2 V 6 V 2 IX 5 V 6 V 2 II 6	07 40 40 40 40 40 40 40 40 40 40 40 40 40	grammes. 1200 1620 1649 1710 1928 2120 2120 2170 2175 2215 2457 2609 2615 2641 2715 2840 2875 2900 3112	c.c. 60·3 81·0 76·3 76·2 88·8 88·8 98·1 87·8 113·9 97·6 89·8 113·8 87·1 121·6 103·2 124·2 116·8 124·5	6.6. 63·4 77·6 78·5 80·3 87·1 92·8 94·1 94·2 95·3 106·3 106·4 107·3 119·5 113·6 114·2 119·8	per cent. 4 · 89 4 · 38 2 · 80 5 · 10 1 · 95 4 · 31 5 · 71 6 · 70 20 · 90 2 · 42 12 · 21 7 · 06 18 · 12 13 · 32 5 · 58 10 · 40 1 · 23 2 · 28 3 · 92	6.6. 52·1 70·3 71·6 74·2 83·7 92·0 94·2 94·4 96·1 106·6 113·2 113·5 114·6 117·8 123·3 124·8 125·9 135·1	per cent. 15·78 15·21 6·56 2·69 6·09 3·48 6·63 6·79 20·64 1·56 15·78 0·53 23·24 6·11 12·41 0·73 10·20 7·23 7·85
	1	1	The second secon	Aver	rage	7.01		8.21

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

Table XV*.

Group.	Rabbits from Table XIII included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood constant, \dagger $k (= W^{2}/B)$.	Blood volume† expressed as percentage of body weight.
A B C D	1—4 5—9 10—14 15—19	grammes. 1545 2103 2507 2888	$\begin{array}{c} \text{c.c.} \\ 76 \cdot 0 \\ 95 \cdot 5 \\ 102 \cdot 0 \\ 116 \cdot 2 \end{array}$	1 · 76 1 · 72 1 · 81 1 · 74	4·92 4·54 4·07 4·02
	<u> </u>	1	Average	1.76	4.39

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

[†] The figures in these columns are calculated from the average body weight and the average blood volume of the group.

Group.	Rabbits from Table XIII included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood volume calculated, $B = W^{\frac{3}{2}}/k$. (Average k for the groups, 1·76.)	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (4·39) of body weight.	Difference between blood volume calculated and observed.
A B C D	14 59 1014 1519	grammes. 1545 2103 2507 2888	$\begin{array}{c} \text{c.c.} \\ 76 \cdot 0 \\ 95 \cdot 5 \\ 102 \cdot 0 \\ 116 \cdot 2 \end{array}$	c.e. 76·0 98·9 104·6 115·4	per cent. 0·00 3·44 2·49 0·69	c.c. 67·8 92·3 110·1 126·8	per cent. 12:10 3:47 7:36 8:36
			Av	erage	1.66		7 ·82

TABLE XVI*.

figures calculated according to the two methods and the observed figures. Calculated as a function of the surface, the average percentage deviation of the blood volume is only 1.66 per cent., but if the blood volume be calculated as percentage of body weight, the average deviation between the calculated and observed figures is 7.82 per cent. In other words, the deviation on the latter plan of calculation is more than four times as great as when the blood volume is calculated as a function of the surface.

Tables XVII to XX deal with the results which ABDERHALDEN obtained upon the blood volume of rabbits which were taken from Basle to St. Moritz, and after living for from 4 to $8\frac{1}{2}$ weeks at the latter place were brought back to Basle. In these tables are included only those animals which were experimented upon after they had been back in Basle for three days or more.

In Table XVII are given the weights, blood volumes, and hæmoglobin percentages of the animals, and our calculations of the blood constants $k = W^{\sharp}/B$, and the blood volumes in percentages of body weight. The average blood constant is found to be 1.58, while the average blood percentage is 4.64 per cent.

In Table XVIII are calculated the blood volumes from the average blood constant (1.58), and from the average blood percentage (4.64), as well as the percentage difference between calculated and observed values in each case. Here, again, it will be seen that the average deviation is smaller when the blood volume is calculated according to our formula (6.00 per cent.) than if calculated as percentage of the body weight (6.49 per cent.).

To bring out more convincingly the real differences shown by the two methods of calculation, we have arranged the animals in four groups in Table XIX, and the

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

TABLE XVII*.

No.	Reference in ABDER- HALDEN'S paper.	Sex.	Body weight. ("Rohgewicht.")	Blood volume observed.	Hæmoglobin (as given by Abder- HALDEN).	Blood constant, $k = W^{\frac{2}{3}}/B$).	Blood volume as percentage of body weight.
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	XI 3 X 8 IV 1 III 5 I 1 IX 7 VII 6 IX 1 VII 1 VII 4 VI 3 I 4 VI 6 II 7 V 3	0, 40 40 40 40 40 40 40 40 40 40 40	grammes. 1815 1895 2175 2445 2470 2514 2545 2705 2715 2715 2855 3025 3040 3050 3235	c.c. 89·2 89·3 115·6 112·1 127·5 111·6 108·6 114·0 140·8 121·1 125·3 145·5 138·1 129·9 140·9	$12 \cdot 23$ $13 \cdot 01$ $11 \cdot 61$ $13 \cdot 25$ $11 \cdot 01$ $12 \cdot 64$ $11 \cdot 84$ $11 \cdot 76$ $13 \cdot 46$ $14 \cdot 01$ $13 \cdot 21$ $13 \cdot 64$ $13 \cdot 72$ $12 \cdot 97$ $13 \cdot 12$	1·67 1·71 1·46 1·62 1·44 1·65 1·72 1·70 1·38 1·61 1·61 1·44 1·52 1·62 1·55	4·92 4·71 5·31 4·59 5·16 4·44 4·27 4·20 5·19 4·46 4·39 4·81 4·54 4·26 4·36
analog and a second			Averaş	ge	$12 \cdot 77$	1.58	4.64

^{*} Abderhalden's experimental data are printed in light type. The figures calculated by us are printed in heavy type.

Table XVIII*.

No.	Reference in Abder- Halden's paper.	Sex.	Body weight. ("Rohgewicht.")	Blood volume observed.	Blood volume calculated. B = $W^{\frac{1}{2}}/k$. $(k = 1.58.)$	Difference between blood volume calculated and observed.	Blood volume calculated as per cent. (4.64) of body weight.	Difference between blood volume calculated and observed.
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	XI 3 X 8 IV 1 III 5 I 1 IX 7 VII 6 IX 1 VII 1 VII 4 VI 3 I 4 VI 6 II 7 V 3	5 50 5 5 50 5 5 5 5 5 5 5 5 5 5 5 5 5 5	grammes. 1815 1895 2175 2445 24470 2514 2545 2705 2715 2715 2715 2855 3025 3040 3050 3235	c.c. 89·2 89·3 115·6 112·1 127·5 111·6 108·6 114·0 140·8 121·1 125·3 145·5 138·1 129·9 140·9	0.6. 94·1 97·0 106·2 114·8 115·9 116·8 118·0 122·8 123·4 123·4 123·3 132·7 133·2 138·3	per cent. 5 · 21 7 · 94 8 · 85 2 · 35 10 · 00 4 · 46 7 · 96 7 · 16 14 · 10 1 · 86 1 · 73 9 · 96 4 · 07 2 · 48 1 · 88	0.0. 84·2 87·9 100·9 113·5 114·6 118·1 125·5 126·0 126·0 132·5 140·4 141·1 141·5 150·1	per cent. 5 · 94 1 · 59 14 · 58 1 · 23 11 · 28 4 · 29 8 · 05 9 · 16 11 · 74 3 · 89 5 · 44 3 · 64 2 · 13 8 · 20 6 · 13
		MARKET MERCELLA A P. CO	× ·	Avera	ge	6.00		6.49

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

blood constant, and blood volume as percentage of body weight, are calculated from the average figures of the groups.

Group.	Rabbits from Table XVII included in group.	Average body weight. ("Rohgewicht.")	Average blood volume observed.	Blood constant, \dagger $k (= \mathrm{W^{2}/B}).$	Blood volume† expressed as percentage of body weight.
A B C D	1—3 4—7 8—11 12—15	grammes. 1962 2494 2748 3088	c.e. 98·0 115·0 125·3 138·6	1 · 60 1 · 60 1 · 57 1 · 53	4·99 4·61 4·56 4·49
		A	Average	1.58	4.66

TABLE XIX*.

The average blood constant of the groups is 1.58, and the average blood percentage is 4.66 per cent. Here, again, there is a regular decrease in the blood as percentage of body weight as the animals increase in weight.

TABLE XX*.

In Table XX are calculated the blood volumes from the average blood constant of the groups (1.58), and from the average blood percentage of the groups (4.66 per

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

[†] The figures in these columns are calculated from the average body weight and the average blood volume of the group.

^{*} ABDERHALDEN'S experimental data are printed in light type. The figures calculated by us are printed in heavy type.

cent.). The percentage deviation between the calculated and observed figures is, in the two cases, 1.62 and 3.51 per cent. It will be seen that the average percentage deviation between the calculated and observed figures is, as usual, much greater when the blood volume is calculated as percentage of body weight than when it is calculated as a function of the surface.

If the average blood constant is calculated from the great number of rabbits which were kept at Basle as controls, it will be found to be 1.60, and the blood volume expressed as per cent. of body weight to be 4.64 per cent.

If we compare Abderhalden's results on rabbits which were kept as controls at Basle with those on rabbits which were brought back to Basle after having been at St. Moritz, it will be found that they have practically the same blood constant in the two cases (1.60 and 1.58). Hence, it appears that after three days in Basle, the rabbits which had been at St. Moritz had regained the same blood volume as the control animals.

There is, therefore, complete and striking agreement between the results which ABDERHALDEN obtained on his great number of Basle rabbits and the results which we published in our last paper, the blood constant $k = W^{\$}/B$ being practically identical in both cases—in the case of ABDERHALDEN's two sets of Basle rabbits 1.60 and 1.58 respectively, and in the case of our own 1.58, a difference of about 0.60 per cent.

ABDERHALDEN'S results are, it will be noticed, entirely different, as were our own, from the results obtained on rabbits by Douglas and by Boycott and Douglas (using the CO method as employed by Haldane and Lorrain Smith), in that they find a much larger blood volume, the average blood constant calculated from their experiments being 1.40, and the blood volume expressed as a percentage of body weight 5.27 per cent. Comparing this with Abderhalden's constant (1.59) and blood percentage (4.64 per cent.), it is seen that they find about 13 per cent. more blood than either Abderhalden or ourselves, and that this is the case whether the blood volume be calculated as a function of the surface or as a percentage of the body weight.

It is further to be seen from Abderhalden's experiments that there is no definite difference in the blood volume of males and females, the average blood constant being practically the same in both sexes. This is in agreement with the results (already published) of our own experiments, pregnant animals being, of course, excluded.

In our last paper we drew attention to the fact that the power $\frac{2}{3}$ in our formula for the blood volume was only approximately correct. This is shown by the fact that if the animals be grouped together the constant shows a tendency towards a slight increase in the light-weight groups compared with its size in the heavy-weight groups when the weights of the animals cover a sufficiently large range. At the same time we pointed out that if the body surface be calculated from the body weight according to Meeh's formula ($S = k \cdot W^{\frac{1}{2}}$) the power $\frac{2}{3}$ in this case is only

approximately correct also, as here, too, the constant k in this formula shows a tendency to be slightly smaller in the lighter animals than in the heavier ones. In both cases, as we have already pointed out, the slight periodical change disappears if the power $\frac{2}{3}$ be replaced by a slightly greater one (0.71–0.72). At the same time we also pointed out that the power $\frac{2}{3}$ is sufficiently accurate for all practical purposes and was adopted by us as being much more convenient for calculation.

To make clear the influence of slightly increasing the power $\frac{2}{3}$ in calculating the surface we have introduced Tables XXI, XXII, and XXIII.

Group.	Subjects from Meeh's table included in group.	Average body weight. ("Roh- gewicht.")	Average body surface.	Surface calculated. S = W ⁿ .k. $n = \frac{2}{3}$. $k = 12 \cdot 23$.	Difference between surface calculated and observed.	Surface calculated. $S = W^n.k'$. $n = 0.73$. $k' = 6.40$.	Difference between surface calculated and observed.	$(S = W^n.k),$ where $n = \frac{2}{3}.$	$(S = W^n.k'),$ where $n = 0.73.$
A B C	1—4 5—8 11, 12, 13, 16 9, 10, 14, 15	grammes. 8,224 20,966 48,219 66,375	sq. cms. 4,587·5 9,311·0 17,443·7 20,067·8	sq. cms. 4,983 9,298 16,200 20,040	per cent. 7 · 92 0 · 14 7 · 68 0 · 14	sq. cms. 4,615 9,139 16,780 21,190	per cent. 0.59 1.88 3.96 5.30	11·26 12·25 13·16 12·24	6·36 6·52 6·65 6·06
		1	Avera	ge	3.97		2.94	12.23	6.40

TABLE XXI*.

In Table XXI, dealing with the experiments on the surface of man as measured by Meeh, the results obtained by this observer on 16 human beings weighing from 3020 grm. to 65,500 grm. are arranged in four groups by averaging the weights and surfaces of the members of each group. From the average weights and surfaces the two constants k and k' are calculated from the power n represented by $\frac{2}{3}$ and the "best n" 0.73, respectively ("best n" meaning here the power which for each species gives the smallest average percentage deviation between the calculated and observed figures). At the same time are calculated the percentage differences between the figures calculated with $n=\frac{2}{3}$ and n=0.73, and the observed values. The average percentage deviation in the two cases is 3.97 per cent. and 2.94 per cent., which is a very marked improvement in the method of calculation and makes the result very nearly, and for all practical purposes, as good as if we introduce into the surface calculation, not only the weight, but also the length and girth, as has been done by MIWA and STOELTZNER. In this case the average percentage difference between the calculated and observed surfaces is 2.67 per cent. If the measurements on man be dealt with individually the "best n" reduces the average percentage difference between calculated and observed figures from 3.60 to 3.12 per cent.

^{*} MEEH's experimental data are printed in light type. The figures calculated by us are printed in heavy type.

In further illustration of this point are given in Tables XXII and XXIII the results of the determination of the surface of guinea-pigs and mice of greatly varying weight which have been made by us.

TABLE XXII.

No.	Body weight. ("Roh- gewicht.")	Surface area observed.	Surface calculated $S = W^{n}.k$. $n = \frac{2}{3}$. $k = 9.56$.	Difference between surface calculated and observed.	Surface calculated. $S = W^n.k'.$ n = 0.72. k' = 7.03.	Difference between surface calculated and observed.	(S = $\mathbb{W}^n . k$), where $n = \frac{2}{3}$.	k' . $(S = W^n.k')$, where $n = 0.72$.
1 2 3	grammes. 148 320 650	sq. cm. 252 459 740	sq. cm. 265 · 7 447 · 3 717 · 4	per cent. 5 · 79 2 · 62 3 · 15	sq. cm. 256 · 8 447 · 4 745 · 2	per cent. 1 · 87 2 · 59 0 · 70	9·01 9·81 9·86	6·90 7·21 6·98
	Avera	age	A CONTRACTOR OF THE CONTRACTOR	3.85		1.72	9.56	7.03

TABLE XXIII.

No.	Body weight. ("Roh- gewicht.")	Surface area observed.	Surface calculated. S = $W^n k$. $n = \frac{2}{3}$. $k = 10.50$.	Difference between surface calculated and observed.	Surface calculated. $S = W^n.k'.$ n = 0.69. k = 9.86.	Difference between surface calculated and observed.	(S = $W^n \cdot k$), where $n = \frac{2}{3}$.	(S = W^n , k'), where $n = 0.69$.
$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	grammes. 10·66 17·46 19·73	sq. cm. 50·5 71·0 77·0	sq. cm. 50·37 70·66 76·68	per cent. 0·26 0·48 0·42	sq. cm. 50·48 70·94 77·20	per cent. 0.04 0.08 0.26	10·42 10·55 10·54	9·87 9·87 9·84
	Avera	ıge		0.39		0.13	10.50	9.86

The weight, as usual, means "Rohgewicht" in grammes, and the surfaces were determined by carefully skinning the animals, making accurate drawings of the skin and determining the surface thus marked out both by planimeter and by the weight of the cut out area of paper, both methods giving the same results. In both Tables XXII and XXIII it will be seen, as in the case of man, that if the power $\frac{2}{3}$ be used the constant k gradually increases as the animals increase in weight, whilst this is not the case if the best n (being in the two cases 0.72 and 0.69) be chosen. Using the two different powers $(n = \frac{2}{3} \text{ and } n = \text{best } n)$, the average percentage deviation between the calculated and observed figures is, in the case of the guineapig, 3.85 per cent. and 1.72 per cent. respectively, while in the case of the mouse it

is 0.39 per cent. and 0.13 per cent. It is to be noted further that the average best n in the three species is between 0.71 and 0.72, exactly as will be seen when the best n for the blood volume is determined.

Having shown the effect of slightly increasing the size of "n" in the case of Meeh's formula, we will return to our own experiments upon the blood volume, and show the similar effect of slightly increasing the power $n = \frac{2}{3}$ in the formula for calculating the blood volume (B = Wⁿ/k).

	Best n.	Average	percentage	Constants.		
Animal.		$n=rac{2}{3}$.	Best n .	Percentage, body weight.	$n=\frac{2}{3}$.	Best n.
Rabbit, tame	0.72	4.61	4.50	9.11	1.58	2 · 37
Guinea-pig	0.71*	4.57	4.28*	$9\cdot 27$	$3 \cdot 30$	4.28
Mouse	0.72	6.65	$6 \cdot 32$	8.61	$6 \cdot 70$	7.85
Hare	0.63	4.05	$3 \cdot 78$	$6 \cdot 15$	0.94	0.70
Rabbit, wild	0.72	3.81	$3 \cdot 81$	4.55	$2 \cdot 04$	3.00
Rat, wild	0.72	4.38	$3 \cdot 88$	6.98	$3 \cdot 05$	4.13
Average	· · ·	4.68	4 · 43	7 · 45		

TABLE XXIV.

In Table XXIV are given the average percentage deviations (for the individual observations within each species) between the figures calculated when n is taken as $\frac{2}{3}$ and when the best n is used and the observed values. There is also appended the average percentage deviation for each species when the blood volume is calculated as percentage of body weight. As the value of k in the formula $k = W^n/B$ necessarily alters greatly with relatively small changes in the size of n, there is also given the value of k when $n=\frac{2}{3}$, and also for k when the "best n" is used. From this table it will be seen, firstly, that the best n does not vary in the different species of animal, as it is in all cases practically the same (0.71 or 0.72), there being but one exception, the hare, where it is slightly less than $\frac{2}{3}$. No stress, however, can be laid upon this, as the observed animals of this species only cover a small range of weight. Secondly, it will be seen that in each species of animal the average percentage deviation between the calculated and observed blood volumes for the individual experiments is only slightly smaller in the case of "best n" than it is in the case of $n=\frac{2}{3}$. The average percentage deviation of all the species is, for the best n, 4.43 per cent., and with $n=\frac{2}{3}$, 4.68 per cent. On the other hand there is a great difference if the blood volume be calculated as percentage of body weight, as here the average percentage deviation for all the species is 7.45 per cent.

Thus for all practical purposes, when individual animals are dealt with the

^{*} With n = 0.72 the deviation is 4.33 per cent. and the constant 4.55.

power $\frac{2}{3}$ is sufficiently accurate, as the best n (0.71 or 0.72) in this case only lessens the percentage deviation slightly.

If, however, we wish to bring out clearly from a theoretical point of view how much smaller the actual difference between calculated and observed values is when the blood volume is calculated as a function of the surface, compared with the percentage deviation when calculated as percentage of body weight, it is essential to make use of the power n which gives the best results when the animals are grouped according to their weight within each species, so as to reduce or eliminate the effect of individual errors as much as possible.

Table XXV.

*	Species.	Best n.	Average percentage deviation with		Constants.		Heaviest group		Deviation by weight.	
Observer.			$n=\frac{2}{3}$.	$\operatorname{Best}_{n.}$	Percentage, body weight.	$n=\frac{2}{3}.$	$\left \begin{array}{c} \operatorname{Best} \\ n. \end{array}\right $	in terms of lightest.		
DREYER and	Rabbit,	0.72	$2 \cdot 77$	2.08	11.91	1.59	2 · 37	4.53	$\begin{array}{c} \text{per cent.} \\ 4 \cdot 30 \end{array}$	$\begin{array}{c} \text{per cent.} \\ 5 \cdot 37 \end{array}$
RAY	tame Guinea-	0.71	$1 \cdot 92$	0.91	10.87	3 · 29	4.28	3 · 37	5.66	11.96
	pig Mouse	0.71	1.35	1.06	$6 \cdot 38$	6.68	7.36	2.00	$4 \cdot 73$	6.02
	Rabbit,	0.72*	0.53	0.16*	$2 \cdot 43$	2.04	3.00	1.29	$4\cdot 59$	15.20
	wild Rat, wild	0.72	1.59	0.92	$5 \cdot 71$	3.04	4.12	1.91	$3 \cdot 59$	6 · 20
RANKE	Rabbit	0.72	4.79	$3 \cdot 72$	$13 \cdot 92$	2.55	3.64	4.72	$2 \cdot 77$	3.58
ABDERHALDEN	Rabbit†	0.72	1.62	0.88	3.51	1.58	$2 \cdot 39$	1.57	$2 \cdot 16$	3 · 99
	Average		2.08	1 · 39	7 · 82		'		3.97	7 · 53

^{*} With n = 0.73 the deviation is 0.00 per cent., and k, 3.22.

Table XXV is similar in structure to Table XXIV, but refers to the grouped animals of each species, including our own experimental results as well as those of Ranke and Abderhalden as calculated by us. Here again the best n is 0.71-0.72. The average percentage deviation between the calculated and observed figures is here smaller with the best n than it is with $n = \frac{2}{3}$, the average of the seven series of experiments being in the two cases 1.39 against 2.08 per cent. Note that the average percentage deviation for all the groups is 7.82 per cent. if calculated as per cent. of body weight.

[†] Refers to the experiments carried out at Basle on rabbits which had been at St. Moritz (see Tables XVII to XX).

We have found that the best n for the calculation of the surface by MEEH's formula ($S = k ext{.}$ W*) in the mammal, taking man, guinea-pig, and mouse as examples, is not $\frac{2}{3}$, but, on an average, 0.71-0.72, exactly as is the case if the blood volume be calculated from the body weight according to our formula. It is therefore clear from the above table that the average percentage deviation between the calculated and observed figures for the above series of animals when the blood volume is calculated as percentage of body weight is from $5\frac{1}{2}$ to $7\frac{1}{2}$ times as great as it is when calculated as a function of the surface according to our formula, using the best n, and four times as large when n is taken $= \frac{2}{3}$.

For all experimental work, whether physiological, pharmacological, or pathological, where the blood volume is concerned, it is necessary to know, not only what the absolute blood volume is in normal animals of a given species, but also, what is equally important, the magnitude of the deviations from the average which may be met with in normal and healthy individuals, since otherwise it is impossible to decide whether the blood volume found by experiment is to be considered normal or abnormal. As we have now examined the blood volumes in a series of 72 mammals of six different species by a uniform and accurate procedure, we believe ourselves to be in a position to state what variations from the average may be met with in normal animals (vide Table XXVI).

TABLE XXVI.

Species.	Mean deviation $(n = \frac{2}{3}).$	Mean deviation (best n).	
Rabbit, tame	5·46 9·03 5·11	$\begin{array}{c} \text{per cent.} \\ 6 \cdot 02 \\ 5 \cdot 09 \\ 8 \cdot 91 \\ 4 \cdot 73 \\ 4 \cdot 54 \end{array}$	
Rat, wild		5.11	

This table gives the *mean* deviations, as calculated by the method of least squares, for each of the six species of animals which we have examined, when the blood volume is expressed as a function of the surface (B = W^{\sharp}/k). The average of the *mean* deviation for the six species is 5.97 per cent. if the power n is taken as $\frac{2}{3}$, and slightly smaller (5.73 per cent.) if the best n (0.71—0.72) is taken.

In Table XXVII we have given in percentages the cases in which the deviation falls within $\frac{1}{2}$, 1, $1\frac{1}{2}$, 2, 3, and 4 times the mean deviation, as well as the theoretical value of these percentages according to the law of the distribution of errors, using the method of least squares. It will be seen that, as regards the distribution of errors,

the agreement between the theoretical values and the values calculated from our experimental results is extremely good. It is therefore evident that it is justifiable to apply the method of least squares to our experimental results on the blood volume of mammals in order to calculate the *mean* deviation.

TABLE XXVII.

	Theoretical distribution. Values.	Distribution found when $n = \frac{2}{3}$.	Distribution found when best n is used.
$\frac{1}{2}$ mean deviation 1 , , , , , , , , , , , , , , , , , , ,	 per cent. $38 \cdot 3$ $68 \cdot 3$ $86 \cdot 6$ $95 \cdot 4$ $99 \cdot 7$ $99 \cdot 994$	per cent. 37.5 68.4 87.3 95.8 98.5 100.0	per cent. 40.2 75.0 86.1 95.8 98.5 100.0

As the mean deviation is about 6 per cent, this indicates that, if an individual animal is found by a reliable method to contain 12 per cent, more or less blood than it should if its blood volume were calculated from the surface, the average constant of the species being used, it is probable that the blood volume of the animal is abnormal, and, if it is 20 per cent, smaller or larger, it is almost certain that the blood volume is abnormally large or small. It may be pointed out, however, that if the blood volume were expressed as a percentage of body weight, it would only be possible to say with the same degree of certainty that the blood volume of an animal was abnormal, when it differed by at least 40 per cent, from the calculated figure.

Finally, it is of interest to point out that if the mean deviation for the hæmoglobin percentage be calculated for the same animals (which, of course, have lived under similar conditions), by the method of least squares, it is found to be 8 per cent. It is therefore evident, as we noted in our previous paper, that animals of the same species living under similar conditions vary less as regards their blood volume than they do as regards their hæmoglobin percentage.

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